Detection of Constrained Unknown Beacon Signals of Terrestrial Transmitters and LEO Satellites with Application to Navigation

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Abstract—Detection of unknown beacons of signals of opportunity (SOPs), whether terrestrial or from low Earth orbit (LEO) satellites is considered. The abundance of SOPs promises an attractive alternative to global navigation satellite system (GNSS) signals. However, some specifications of ambient SOPs may not be available to the public. In this paper, a computationally efficient cognitive opportunistic navigation framework is proposed to (i) detect constrained unknown beacons and (ii) estimate their Doppler frequencies. Experimental results are presented demonstrating the efficacy of the proposed framework in successful detection and Doppler tracking for both terrestrial cdma2000 signals and Orbcomm LEO satellite signals.

I. INTRODUCTION

Signals of opportunity (SOPs) have been considered as an alternative to global navigation satellite systems (GNSS) [1], [2]. While some SOPs openly publish their specifications (e.g., cellular signals are described in 3GPP standards [3]), other SOPs do not make such information publicly available (e.g., low Earth orbit (LEO) satellite signals [4]). This makes acquiring and tracking the latter SOPs impossible.

Cognitive opportunistic navigation addresses this challenge via blind estimation of signal characteristics [5]. Assuming that the SOP follows a standard modulation scheme (e.g., phase shift keying (PSK) or quadrature amplitude modulation (QAM)) and a standard multiple-access technique (e.g. code-division multiple access (CDMA) or orthogonal frequency-division multiplexing (OFDM)), a cognitive opportunistic navigation receiver recovers the unknown signal structure, to exploit the signal and produce a navigation solution. Most communication systems employ a synchronization beacon signal for timing and carrier offset recovery. For example, in cellular CDMA, pseudorandom noise (PN) sequences are used on the forward-link pilot channel for synchronization proposes [6]. Other examples are the primary synchronization signal (PSS) and secondary synchronization signal (SSS) in cellular long-term evolution (LTE) and 5G systems [7], [8]. While different broadband services may use the same modulation schemes, their underlying configuration and parameters could differ. For instance, the Globalstar satellite system supposedly uses similar protocol to the IS-95 and cdma2000 cellular CDMA system but with different PN sequences [6]. Although the Globalstar system is in lot of ways similar to the cdma2000 system, Globalstar satellite signals cannot be acquired without knowing the corresponding PN sequences [9]. Preliminary experiments for navigation with partially known signals were conducted in [10]–[13]. In [14], unknown Starlink satellite signals were exploited for navigation for the first time.

The detection problem of an unknown source in the presence of other interfering signals falls into the paradigm of matched subspace detectors [15]–[17]. In the detection problem of constrained beacons, the integer constraint of the beacon symbols in the matched subspace detectors leads to a class of integer least square problems [18], [19]. One example of a constrained beacon is the PN sequence in CDMA-based communication systems. A low computational complexity approach to estimate the beacon symbols is symbol-by-symbol estimation, which suffers from a poor performance in low signal-to-noise ratio (SNR) regimes. In [20], a symbol-by-symbol estimation scheme was considered to blindly estimate the symbols of the PN sequences of Galileo and Beidou satellites, and a 1.8 m high-gain antenna was used to accumulate enough signal power. The optimal algorithm proposed in [18], [19] can be used to solve the integer least squares problem with a polynomial computational complexity. The computational and hardware complexity of the integer least squares problem are two of the main challenges that should be addressed in a cognitive opportunistic navigation framework. This paper proposes a near optimal beacon detector with linear computational complexity for signals with integer constraint. First, low computational complexity algorithms are proposed to tackle two of the main challenges of opportunistic navigation: blind beacon signal detection and blind Doppler estimation. Second, experimental results are presented demonstrating the efficacy of the proposed framework in successful blind detection and Doppler estimation for both terrestrial cdma2000 signals and Orbcomm LEO satellite signals.

The rest of the paper is organized as follows. Section II overviews the cognitive opportunistic navigation framework and describes the signal model. Section III discusses the proposed beacon detection and blind Doppler estimation algorithms. Section IV presents experimental results. Concluding remarks are given in Section V.
II. COGNITIVE OPPORTUNISTIC NAVIGATION AND BASEBAND SIGNAL MODEL

This section provides an overview of the cognitive opportunistic navigation framework and describes the baseband received signal model on which the framework operates.

A. Framework Overview

A Cognitive opportunistic navigation system mainly relies on blind detection and tracking of beacon signals in broadband communication systems, e.g., detecting the PN sequence in 3G cdma2000 systems or the SSS or PSS in 4G LTE and 5G systems [5]. From limited prior information about a particular broadband system, crucial unknown parameters along with the beacon or pilot signals are estimated, which in turn allows for exploiting received signals for navigation purposes.

A beacon or a pilot signal is a signal known by the receiver and is used for timing and carrier synchronization. Correlation-based receivers are typically used to detect the presence of beacon signals and synchronize to them. These receivers are typically capable of reliably detecting known beacon signals at relatively low SNRs. However, the beacon is unknown to a cognitive opportunistic receiver and the signal’s SNR can be too low for reliable blind detection. As such, coherent integration becomes crucial to increase the effective SNR of the received beacon signal. To coherently integrate successive transmissions of the beacon signal, the Doppler shift (or Doppler frequency) must be estimated. Therefore, the two building blocks of a cognitive opportunistic navigation system are (i) blind Doppler estimation/tracking and (ii) blind beacon detection/tracking. Once a blind estimate of the Doppler is produced, one can perform coherent integration and feed the integrated signal to a detection algorithm to detect and estimate the symbols of the beacon sequence.

B. Received Baseband Signal Model

Let \( s(t) \) denote the beacon signal consisting of \( N \) consecutive symbols with symbol duration \( T_{\text{sym}} \). Each symbol is drawn from an arbitrary \( M \)-PSK constellation. The beacon signal is continuously transmitted at a period of \( N \cdot T_{\text{sym}} \). After channel propagation and baseband sampling at interval \( T_s \), the received signal can be modeled as

\[
y[n] = \sum_{i=-\infty}^{\infty} \alpha \exp(j2\pi fDn) s[n - iL - n_d] + w[n], \quad (1)
\]

where \( y[n] \) is the complex baseband sample at the \( n \)th time slot; \( L = N \frac{T_{\text{sym}}}{T_s} \) is the length of the beacon in samples; \( fD \) is the normalized Doppler frequency and \( f_D \) is the true Doppler frequency in hertz; \( w[n] \) models noise and interference; \( n_d \) is the unknown delay of the received beacon signal; and \( \alpha \) is an unknown complex amplitude. For convenience of notation, define the \( k \)th truncated vector of received samples of length \( L \) as

\[
y^k \triangleq [y[kL], y[kL+1], \ldots, y[(k+1)L-1]]^T. \quad (2)
\]

III. DETECTION OF THE BEACON SIGNAL AND BLIND DOPPLER ESTIMATION

Consider an observation vector \( y^k \) of length \( L \). One can reformulate the system model as

\[
y^k = \alpha d^k \otimes s^k + w^k, \quad (3)
\]

where \( \alpha \) is the unknown complex amplitude of the received signal and is considered to be constant in the coherent processing interval, \( \otimes \) is the Hadamard product, \( w^k \) is an independent and identically distributed (iid) noise with zero mean and variance \( \sigma^2 \), and \( d^k \) captures the effect of the Doppler, i.e.,

\[
d^k = \{\exp(j2\pi fD(kL)), \ldots, \exp(j2\pi fD((k+1)L-1))\}.
\]

Also, consider the set \( \mathcal{L} \) consisting of all \( M^L \) vector combinations whose elements are the integers between 0 and \( M - 1 \). For \( M \)-PSK, a beacon sequence is \( s^k = \exp\left(\frac{2\pi}{M}q\right) \) where \( q \in \mathcal{L} \). The problem of non-coherent blind detection of \( q \) and \( \Delta f \) is addressed in the following subsection.

A. Beacon Signal Detection

One can show that the non-coherent maximum likelihood (ML) detector of \( q \) is

\[
\hat{q}, \hat{\Delta f} = \arg\max_{q \in \mathcal{L}, \Delta f} \left| (d^k) \ast y^k \right|^H \exp\left(\frac{j2\pi}{M}q\right), \quad (4)
\]

where \((\cdot)^\ast\) and \((\cdot)^H\) are the complex conjugate and Hermitian operators, respectively. For convenience, define \( z \triangleq (d^k)^\ast \ast y^k \). A solution to the optimization problem (4) consists of a linear search over Doppler candidates and an exponential brute-force search over all possible values of \( q \). Denoting the number of Doppler search candidates by \( |\mathcal{D}| \), the order of the overall search is \( |\mathcal{D}|M^K \). In an effort to solve (4) in less than quadratic complexity, a technique that has been utilized in [21], [22] will be adopted. The following lemma calculates the reduced number of search candidates.

**Lemma 1:** The optimal solution of the optimization problem (4) can be obtained by searching over \( |\mathcal{D}|L \) candidates.

**Proof:** In order to calculate the number of search candidates, first, rewrite the coherent detector of \( q \) for a given phase complex amplitude \( \alpha \). Note that the coherent detector does not depend on the magnitude of \( \alpha \), but only depends on its phase \( \phi \). More precisely, for a given value of \( \phi \), one has [21]

\[
\{q_\phi, \hat{\Delta f}\} = \arg\max_{q, \Delta f} \Re \left\{ \exp(-j\phi)z^H \exp\left(\frac{j2\pi}{M}q\right) \right\}. \quad (5)
\]

Due to the nature of iid noise and the independence of the elements of \( s^k \), the coherent detector simplifies to a symbol-by-symbol \( M \)-PSK detector for a given \( \Delta f \) and \( \phi \). Hence, the \( k \)th element of \( q_\phi \) is obtained by mapping the phase of the \( k \)th element of \( \exp(j\phi)z \) to the closest multiple of \( \frac{2\pi}{M} \), i.e.,

\[
q_\phi[k] = \text{round}\left( (\phi_k + \phi) \frac{M}{2\pi} \right) \mod M, \quad (6)
\]

where mod is the modulus operator and \( \phi_k \triangleq \arg\{z[k]\} \). Thus, for a given \( \Delta f \), one can find the optimal \( q \) by searching
over all possible values for $\phi$. However, it can be readily shown from (6), that $q_\phi$ and $q_{\phi+\frac{2\pi}{M}}$ result in the same likelihood function in (4). Consequently, the search space for $\phi$ is limited to the interval $[0, \frac{2\pi}{M})$.

Since $\phi$ is limited to the interval $[0, \frac{2\pi}{M})$, a detected MPSK symbol will have an ambiguity of 2 instead of $M$. That is, a particular $q_{\phi}[k]$ can take one of two values, based on which symbol in the MPSK constellation is closest to it. Define $c_1 \triangleq q_{\phi=0}$ and $c_2 \triangleq q_{\phi=\frac{2\pi}{M}}$, where it can be shown through (6) that $c_2[k] = (c_1[k] + 1) \mod M$. It can also be shown using (6) that the boundary angle between two symbols in the MPSK constellation is given by $\gamma_k \triangleq \frac{2\pi}{M} c_1[k] + \frac{2\pi}{M} - \phi_k$. Subsequently, each candidate MPSK symbol will be given by

$$q_{\phi}[k] = \begin{cases} c_1[k], & \phi \leq \gamma_k, \\ c_2[k], & \phi > \gamma_k. \end{cases}$$

(7)

For convenience of notation, sort the values of $\gamma_k$ in an ascending order with a new index $k'$ such that $\gamma_{k'+1} > \gamma_{k'}$. Therefore, the first boundary angle is $\gamma_1$. Consequently, each candidate is of the form

$$[q_{\phi=0}[1] + 1 - u(\gamma_1 - \phi), \ldots, q_{\phi=0}[L] + 1 - u(\gamma_L - \phi)]^T,$$

(8)

where $u(\cdot)$ is the unit step function. Equation (8) implies that for different values of $\phi$, one has $L$ different candidates $A = \{a_1, \ldots, a_L\}$. Each candidate should be plugged in (4) to get the optimal $\hat{q}$. Finally, by searching over Doppler the total number of $|D|L$ search candidates are obtained.

According to Lemma 1, in order to find the candidate effectively, one needs to solve

$$\{\hat{q}, \hat{\Delta f}\} = \arg \max_{q_{\in A}, \Delta f} \left| \left( (d)^* \otimes y^k \right)^H \exp \left( j\frac{2\pi f}{M} q \right) \right|,$$

(9)

where $\text{card}(A) = |D|L$ and $\text{card}(A)$ is the cardinality of the set $A$. Note that according the proof of Lemma 1, by plugging the consecutive candidates $a_i$ in (4), the following recursive formula is obtained, which can be used to solve (4) effectively,

$$z^H \exp \left( j\frac{2\pi f}{M} a_k \right) = z^H \exp \left( j\frac{2\pi f}{M} a_{k-1} \right) + z[l]^* \exp \left( j\frac{2\pi f}{M} \tilde{a}_1[l] \right) \exp \left( j\frac{2\pi f}{M} - 1 \right).$$

(10)

Equation (10) demonstrates the recursion between the likelihood functions corresponding to each candidate. It can be seen from (10) that the $k$th likelihood only depends on the $l$th observation and the previous likelihood. Therefore, a tree based algorithm based on (10) can be employed to optimally detect the beacon sequence with a computational complexity of order $|D|L$.

### B. Blind Doppler Estimation

The performance of the beacon signal detection algorithm, and consequently the accuracy of the cognitive navigation system, depends on the effective SNR. It is essential to account for the Doppler in order to coherently integrate the observations and increase the effective SNR. A blind Doppler estimation (BDE) method is proposed, which is capable of estimating the Doppler even when the beacon sequence is unknown. The main idea of the BDE algorithm is performing a nonlinear operation to remove the beacon sequence from the observation vector and applying the least squares (LS) method to estimate the Doppler via the beacon-free observation. Let us express the actual normalized Doppler frequency as

$$\Delta f = \Delta f_1 + \Delta f_D,$$

(11)

where $\Delta f_1 \triangleq \frac{uf}{M}$ is referred to as the integer part and $\Delta f_D \in [-\frac{1}{2T}, \frac{1}{2T}]$ is referred to as the decimal part of the Doppler. The nonlinear transformation $(y^k)^M$, which raises each element of $y^k$ to the power $M$, produces a term where the beacon sequence is wiped off. The LS estimate of $\Delta f_1$, denoted by $\hat{\Delta f}_1$, boils down to the maximizer of the magnitude of the $L$ point discrete Fourier transform (DFT) of $(y^k)^M$ [23]. After wiping off the integer Doppler from the original observation, which results in the new observation vector $y_D^k$, the decimal part can be estimated by dividing the phase of the inner product $(y_D^k)^H y_D^{k+1}$ by the beacon period.

The details of the BDE method are presented in Algorithm 1. Note that in Algorithm 1, $K$ is the coherent processing interval, i.e., the number of successive frames for which the Doppler frequency is assumed constant.

### Algorithm 1: BDE algorithm

**Input:** $y^k$ for $k = 1, \ldots, K$  
**Output:** $\hat{\Delta f}_1^k$ and $\hat{\Delta f}_D^k$

1. Calculate $\hat{b}^k = \arg \max \left| \left( \text{FFT} \left( (y^k)^M \right) \right) \right|$ for $k = 1, \ldots, K$.
2. Find $\hat{\Delta f}_1^k = \left\{ \frac{\hat{b}^k}{M}, \frac{\hat{b}^k}{M} \right\}$ and $\hat{\Delta f}_D^k = \frac{1}{K} \sum_{k=1}^{K} \hat{\Delta f}_D^k$.
3. Wipe-off the integer part as $y_D^k = \exp(-j2\pi \hat{\Delta f}_1(kL)) \ldots \exp(-j2\pi \hat{\Delta f}_1((k + 1)L - 1)) y^k$.
4. Find the decimal part as $\Delta f_D^k = \frac{1}{K} \arg \left\{ (y_D^k)^H y_D^{k+1} \right\}$ and calculate $\hat{\Delta f}_D^k = \frac{1}{K} \sum_{k=1}^{K} \hat{\Delta f}_D^k$.

### IV. Experimental Results

#### A. Experiment 1: cdma2000 signals

This section presents experimental results for UAV navigation with real cdma2000 signals, using the proposed cognitive opportunistic navigation framework.

1. **Experimental Setup:** A UAV was equipped with an Ettus E312 universal software radio peripheral (USRP) to sample cdma2000 signals, a consumer-grade 800/1900 megahertz cellular antenna, and a small consumer-grade GPS antenna to discipline the on-board oscillator. The receiver was tuned to a 882.75 megahertz carrier frequency, which is a cdma2000 channel allocated for the U.S. cellular provider Verizon Wireless. Samples of the received signals were stored for off-line
post-processing. The ground-truth reference for the UAV trajectory was taken from its on-board navigation system, which uses GPS, an inertial measurement unit (IMU), and other sensors. The UAV’s total traversed trajectory was 1.72 km, which was completed in 3 minutes. Over this trajectory, the receiver on-board the UAV was listening to 4 base transceiver stations (BTSs), whose positions were mapped prior to the experiment. The experimental environment is shown in Fig. 1.

2) PN Sequence Detection Results: Next, the cdma2000 PN sequence is estimated from the forward link signal, as discussed in Section III. A scatter plot of the detected sequence is shown in Fig. 2(a), which seems to be very noisy even though a diamond shape is visible. Fig. 2(b) shows the correlation function between the detected and true cdma2000 forward channel PN sequence, whose clean peak indicates that the detected sequence can be reliably used to despread the cdma2000 signal. The detected PN sequence is then used to acquire and track the cdma2000 signals and produce carrier phase observables using the receiver implementation discussed in [24]. The carrier phase, expressed in meters, gives a measure of the distance between the transmitter and the receiver, up to a certain ambiguity [25]. In order to illustrate the ranging performance with the detected PN sequence, the change in distance with respect to the initial distance, called the delta range, was computed in two ways for each BTS: (i) using the UAV’s and BTSs’ known positions (true) and (ii) from the carrier phase observables obtained with the detected PN sequence (estimate). The results are shown in Fig. 3.

3) Navigation Results: The single-receiver navigation framework developed in [26] was used to produce a navigation solution using the carrier phase measurements from the 4 BTSs. The total position root mean-square error (RMSE) was found to be 74.97 cm over the entire trajectory. The true and estimated trajectories are shown in Fig. 4.

B. Experiment 2: Orbcomm Satellite Signals

This section presents experimental results with Orbcomm LEO satellites on a stationary receiver.

1) Experimental Setup: A stationary receiver was equipped with an Ettus E312 USRP, a very high frequency (VHF) antenna, and a consumer-grade GPS antenna to discipline the on-board oscillator. The receiver was tuned to a 137 MHz carrier frequency with 2.4 MHz sampling bandwidth, which covers the 137–138 MHz band allocated to Orbcomm satellites. The LEO carrier phase measurements were produced at a rate of 4.8 kHz and were downsampled to 10 Hz. Over the course of the experiment, the receiver was listening to 2 Orbcomm satellites, namely FM 108 and FM 116.

2) Beacon Detection and Doppler Tracking Results: Unlike OFDM and CDMA-based signals where the signal power per degree of freedom is small, in classic modulation schemes, e.g., Mary PSK, a relatively larger power is dedicated to each degree of freedom. In other words, the allocated signal power per each time/frequency unit is relatively higher than spread spectrum techniques [27]. The Orbcomm constellation utilizes the classic symmetric differential phase shift keying (SDPSK) as the modulation scheme for downlink signals [28]. SDPSK is defined by a “zero” data state causing $\pi$ phase shift and the “one” data state causing $\pi$ phase shift. In order to increase the effective power of the periodic beacon in the Orbcomm constellation, the observation samples are raised to the power of two, which turns the SDPSK modulated signal into a fixed sequence of binary samples, which is considered as the
reference signal for the proposed receiver. Fig. 5(a) shows the beacon signals of Orbcomm satellite signals. Fig. 5(b) shows the correlation function between the detected beacon signal of the Orbcomm satellite signals with the received signal, whose clean peak indicates that the detected beacon can be reliably used to despread the downlink signal. Fig. 6 compares Doppler tracking results of the two Orbcomm satellites using the proposed method versus the estimated Doppler from two-line element (TLE) files and an SGP4 propagator.

![scatter plot](image1.jpg)

**Fig. 5. (a) Scatter plot of detected beacon signals from Orbcomm satellite. (b) Correlation function between the detected beacon signal and received signal.**

**Fig. 6. Estimated Doppler from two Orbcomm LEO satellites versus the estimated Doppler from TLE files and SGP4 propagator.**

V. CONCLUSION

This paper proposed a cognitive opportunistic navigation framework for constrained beacon signals. First, a low complexity blind detection algorithm was proposed to detect the beacon signal. Second, a blind algorithm was proposed to estimate the unknown Doppler frequency. The proposed framework was demonstrated with (i) cdma2000 signals, achieving submeter-accurate UAV navigation over a 1.72 km trajectory and (ii) two Orbcomm LEO satellites, achieving beacon signal detection and Doppler tracking with a stationary receiver.

REFERENCES


